

MATH 252 EXERCISES for MT2

- 1) Evaluate $\int_0^4 \left(\int_{\frac{y}{2}}^{1+\frac{y}{2}} \frac{2x-y}{2} dx \right) dy$. Use $u = \frac{2x-y}{2}, v = \frac{y}{2}$.
- 2) Evaluate $\int_0^1 \left(\int_0^x \sqrt{x+y} \cdot (y-2x)^2 dy \right) dx$.
- 3) Show that $\vec{F}(x, y, z)$ is conservative, and then evaluate the following integrals.
 - a) $\int_{(0,2,1)}^{(1,\frac{\pi}{2},2)} \cos y dx + \left(\frac{1}{y} - 2x \sin y\right) dy + \frac{1}{z} dz$.
 - b) $\int_{(1,1,1)}^{(1,2,3)} 3x^2 dx + \frac{z^2}{y} dy + 2z \ln y dz$.
- 4) Use Green's Theorem, evaluate $\oint_C xy dx + x^2 y^3 dy$, where C is the triangle with vertices $(0,0), (1,0), (1,2)$ in clockwise.
- 5) Using double integrals, find the area of R bounded by $x + y^2 = 4$ and $y + 2 = x$.
- 6) Reverse the order of integration

$$\int_{-2}^1 \int_{y+2}^{4-x^2} \sin(x^2) dx dy$$
- 7) Use transformation $u = 2x + 3y, v = 2y$ to evaluate the area of the ellipse

$$4x^2 + 12xy + 13y^2 = 3$$
- 8) Evaluate $\int_C xy dx - y^2 dy + xz dz$, where C is the line segment from $(1,1,2)$ to $(0,0,0)$.
- 9) Let $\vec{F}(x, y, z) = (e^x \cos y + yz)\vec{i} + (xz - e^x \sin y)\vec{j} + (xy + z)\vec{k}$.
 - a) Show that $\vec{F}(x, y, z)$ is conservative.
 - b) Find $\int_C \vec{F} \cdot d\vec{r}$ where C is the line segments from $(0,0,0)$ to $(1,0,2)$ to $(2, \pi, 4)$.